

Neural Distributed Image Compression Using Common Information

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¹ Equal contribution.

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Source coding

System Model: Point-to-point

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- Lossless

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- Lossy

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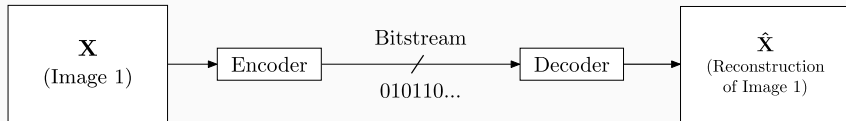
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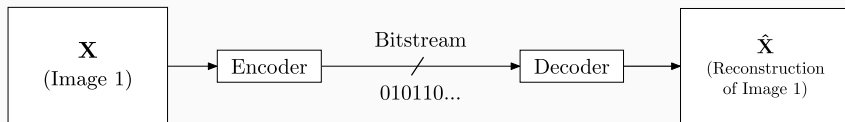


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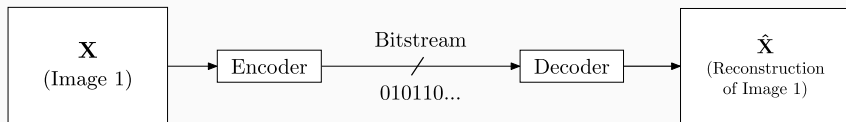
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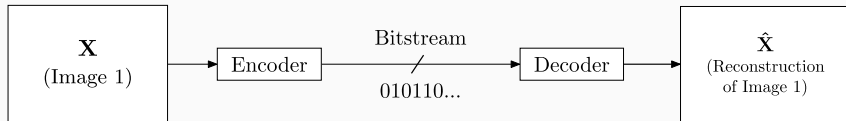
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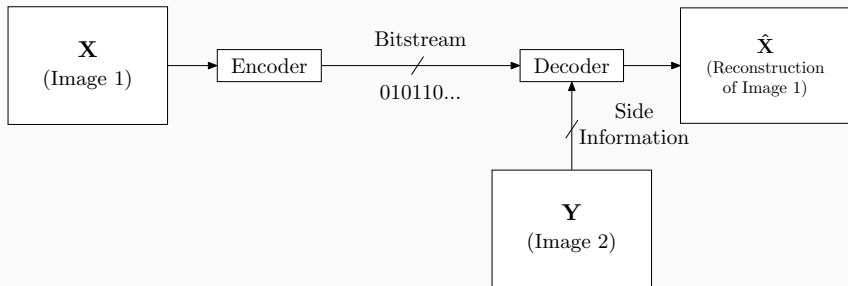
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Two competing goals in lossy compression:

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- Distortion

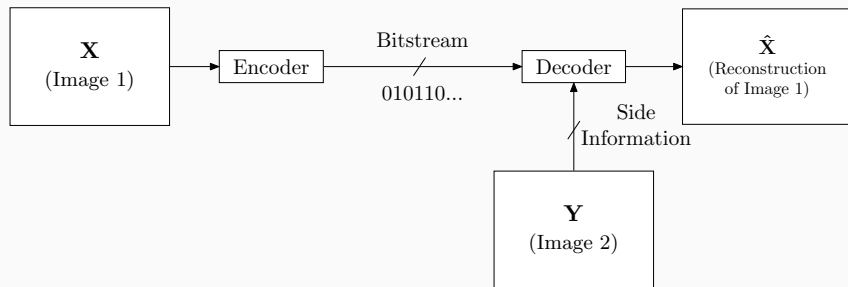
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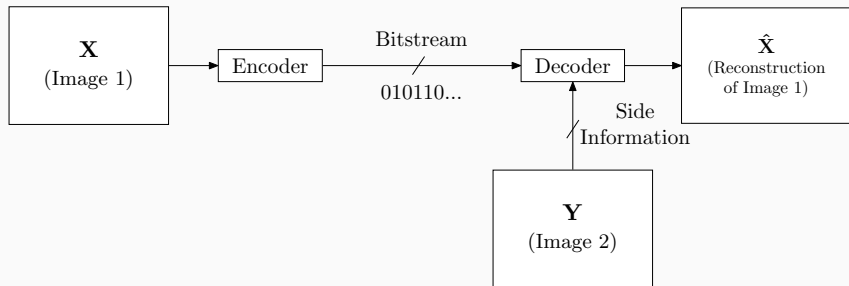
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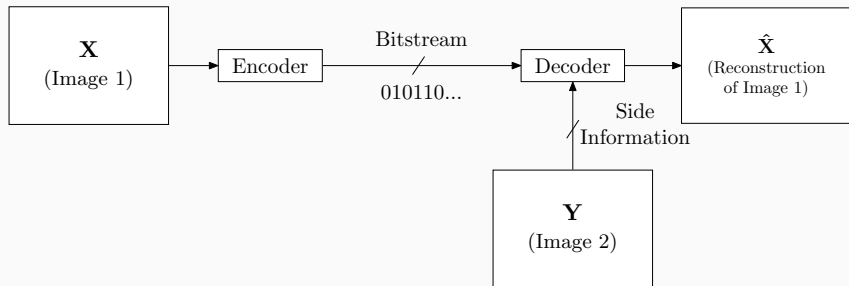
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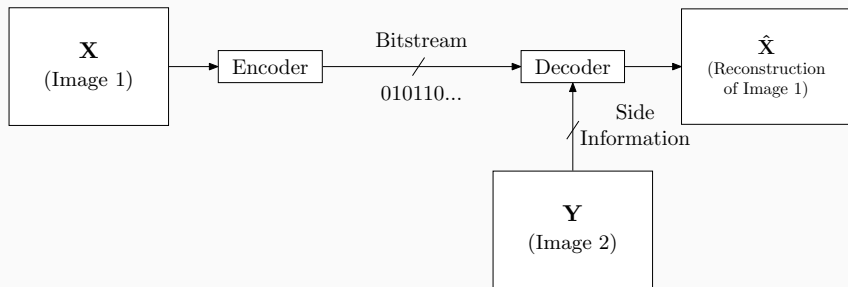
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- [Girod et al., 2005](#) Distributed Video Coding.

Motivation for DSC Setup



Pair of correlated images with overlapping fields of view.

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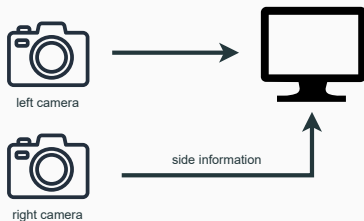
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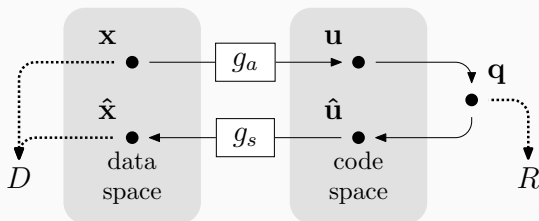
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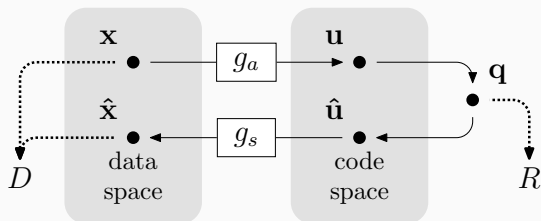
Lossy Compression: Transform Coding



Transform coding framework¹.

¹Figure provided is from Ballé et al., 2017.

Lossy Compression: Transform Coding

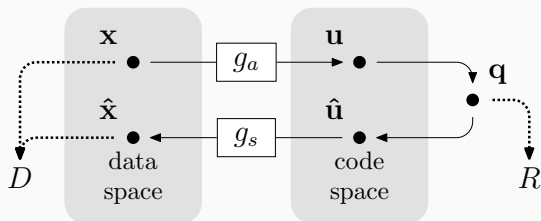


Transform coding framework¹.

$$\begin{aligned} & \min R \\ & \text{subject to } \mathbb{E}[D] \leq D_c \end{aligned}$$

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Lossy Image Compression using DNNs

- [Ballé et. al., 2017](#) Deep end-to-end image compression.

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$$L(\mathbf{g}_a, \mathbf{g}_s) = R + \lambda D,$$

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$$R = \mathbb{E}_{\mathbf{x} \sim p(\mathbf{x})} \underbrace{[-\log p(\tilde{\mathbf{u}} | \tilde{\mathbf{z}})]}_{\text{latent}} + \mathbb{E}_{\mathbf{x} \sim p(\mathbf{x})} \underbrace{[-\log p(\tilde{\mathbf{z}})]}_{\text{hyperprior}}$$

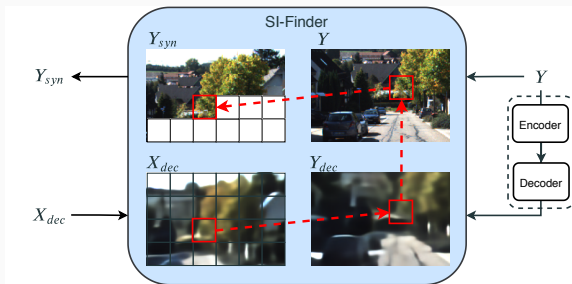
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- [Ayzik and Avidan, 2020](#) (DSIN) - Reconstruct an intermediate image, then find corresponding patches in the side information image, which they use to refine the reconstructed image.

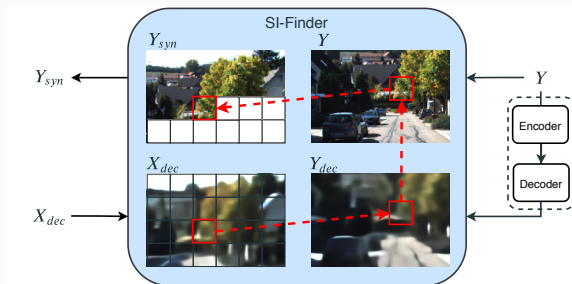
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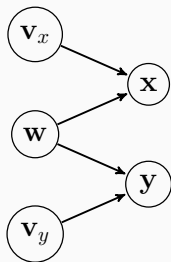
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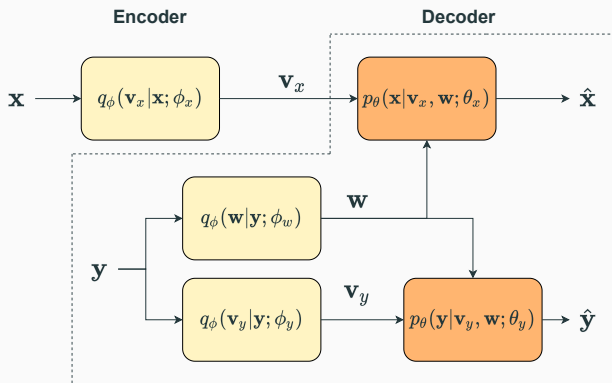
- [Whang et. al., 2021](#) - Transform side information image to a latent space. Use it together with the received latent variable to jointly reconstruct the image.

Proposed Solution

Distributed Source Coding Architecture

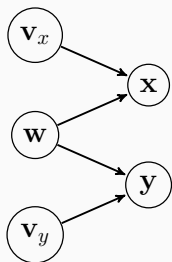


Graphical model. [Wang et al., 2017]

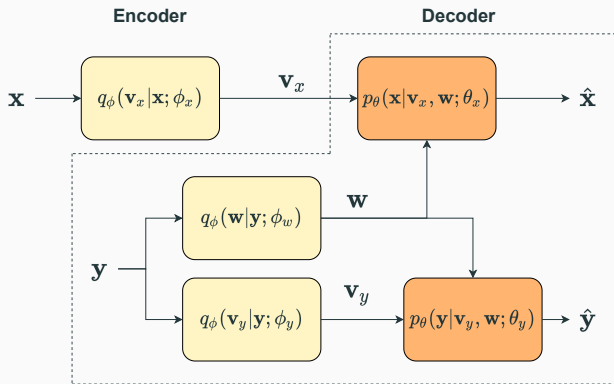


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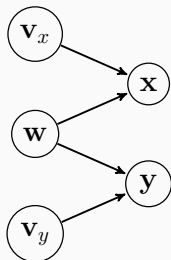


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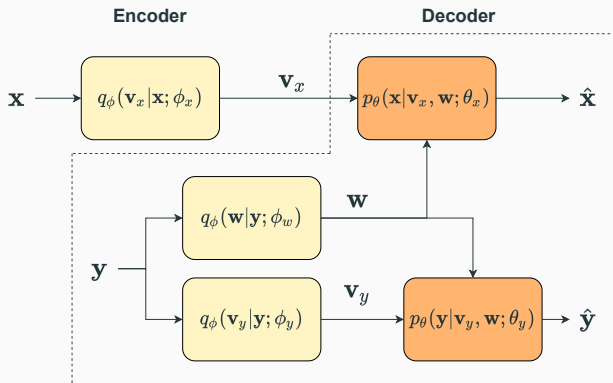
v_x , v_y and w are independent latent variables:

- w - common information.
- v_x and v_y - independent information of x and y .
- Generate x and y as above.

Distributed Source Coding Architecture



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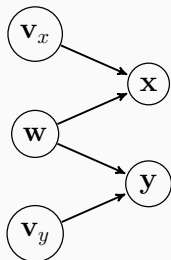


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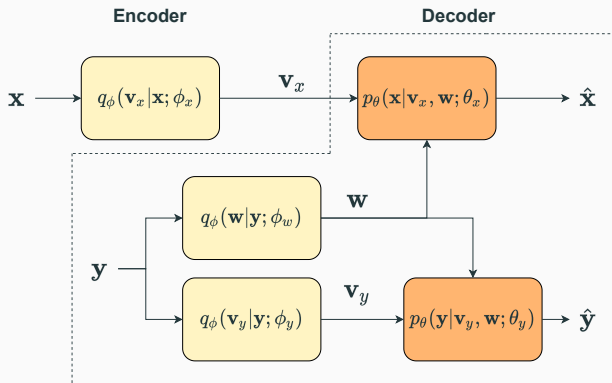
$$p(\mathbf{x}, \mathbf{y}, \mathbf{w}, \mathbf{v}_x, \mathbf{v}_y) = p(\mathbf{w})p(\mathbf{v}_x)p(\mathbf{v}_y)p_\theta(\mathbf{x} | \mathbf{w}, \mathbf{v}_x; \theta_x)p_\theta(\mathbf{y} | \mathbf{w}, \mathbf{v}_y; \theta_y)$$

Factored joint prior distribution of the latent variables emerging from the graphical model.

Distributed Source Coding Architecture



Graphical model. [Wang et al., 2017]



Distributed source coding architecture.

$$q_\phi(\mathbf{w}, \mathbf{v}_x, \mathbf{v}_y | \mathbf{x}, \mathbf{y}) = q_\phi(\mathbf{v}_x | \mathbf{x}; \phi_x) q_\phi(\mathbf{w} | \mathbf{y}; \phi_w) q_\phi(\mathbf{v}_y | \mathbf{y}; \phi_y)$$

Factored variational approximation of the posterior distribution emerging from the system architecture.

$$\min_{\phi, \theta} \mathbb{E}_{\mathbf{x}, \mathbf{y} \sim p(\mathbf{x}, \mathbf{y})} D_{\text{KL}} [q_{\phi}(\tilde{\mathbf{v}}_x, \mathbf{v}_y, \mathbf{w} \mid \mathbf{x}, \mathbf{y}) \parallel p(\tilde{\mathbf{v}}_x, \mathbf{v}_y, \mathbf{w} \mid \mathbf{x}, \mathbf{y})]$$

Loss Function

$$\begin{aligned} & \min_{\phi, \theta} \mathbb{E}_{\mathbf{x}, \mathbf{y} \sim p(\mathbf{x}, \mathbf{y})} D_{\text{KL}} [q_{\phi}(\tilde{\mathbf{v}}_x, \mathbf{v}_y, \mathbf{w} \mid \mathbf{x}, \mathbf{y}) \parallel p(\tilde{\mathbf{v}}_x, \mathbf{v}_y, \mathbf{w} \mid \mathbf{x}, \mathbf{y})] \\ &= \min_{\phi, \theta} \mathbb{E}_{\mathbf{x}, \mathbf{y} \sim p(\mathbf{x}, \mathbf{y})} \mathbb{E}_{\tilde{\mathbf{v}}_x, \mathbf{v}_y, \mathbf{w} \sim q_{\phi}} \left(\left(\log q_{\phi}(\tilde{\mathbf{v}}_x \mid \mathbf{x}; \phi_x) + \log q_{\phi}(\mathbf{v}_y \mid \mathbf{y}; \phi_y) + \log q_{\phi}(\mathbf{w} \mid \mathbf{y}; \phi_f) \right) \right. \\ & \quad \left. - \left(\underbrace{\log p_{\theta}(\mathbf{x} \mid \mathbf{w}, \tilde{\mathbf{v}}_x; \theta_x)}_{D_x} + \underbrace{\log p_{\theta}(\mathbf{y} \mid \mathbf{w}, \mathbf{v}_y; \theta_y)}_{D_y} + \underbrace{\log p(\mathbf{w})}_{R_w} + \underbrace{\log p(\tilde{\mathbf{v}}_x)}_{R_x} + \underbrace{\log p(\mathbf{v}_y)}_{R_y} \right) \right) \\ & \quad + \text{const.} \end{aligned}$$

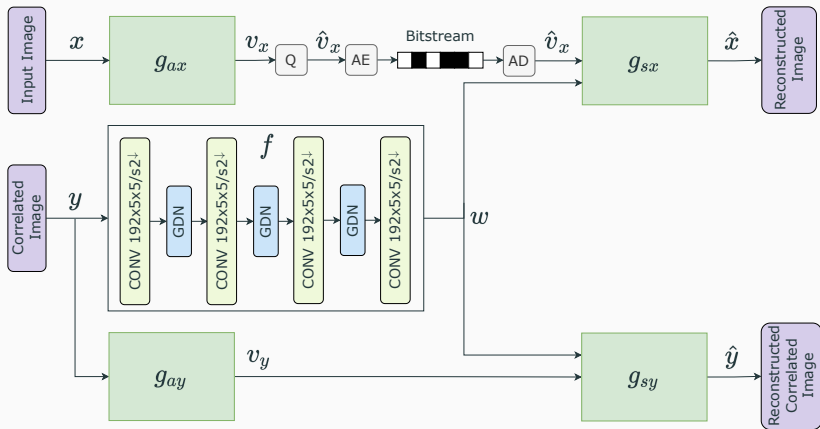
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Adding weights α , β and λ to control the contribution of the terms, we write:

$$L(\mathbf{g}_{ax}, \mathbf{g}_{sx}, \mathbf{g}_{ay}, \mathbf{g}_{sy}, \mathbf{f}) = (R_x + \lambda D_x) + \alpha (R_y + \lambda D_y) + \beta R_w,$$

Neural Network Architecture



Experimental Setup and Results

Datasets

KITTI Stereo

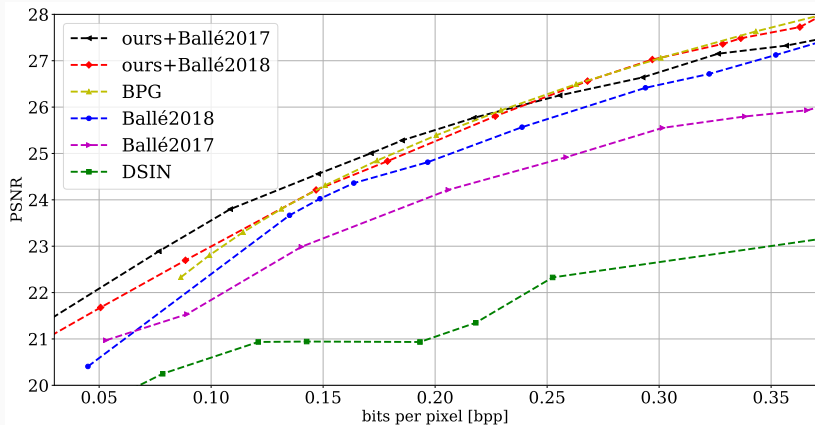


Cityscape



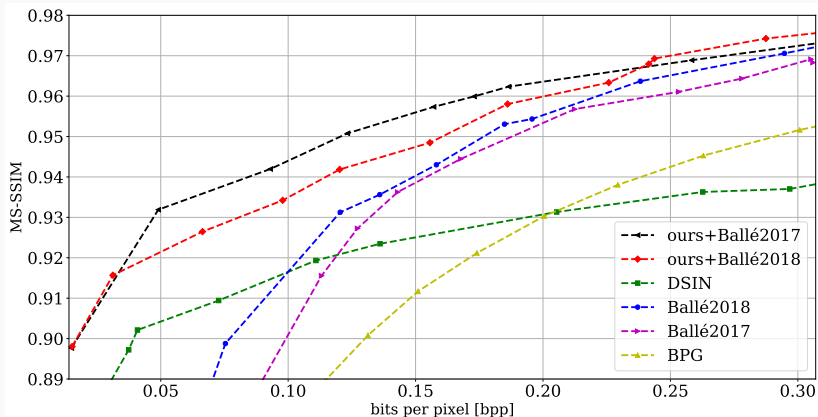
Example stereo image pairs from KITTI Stereo and Cityscape.

Results with KITTI Stereo



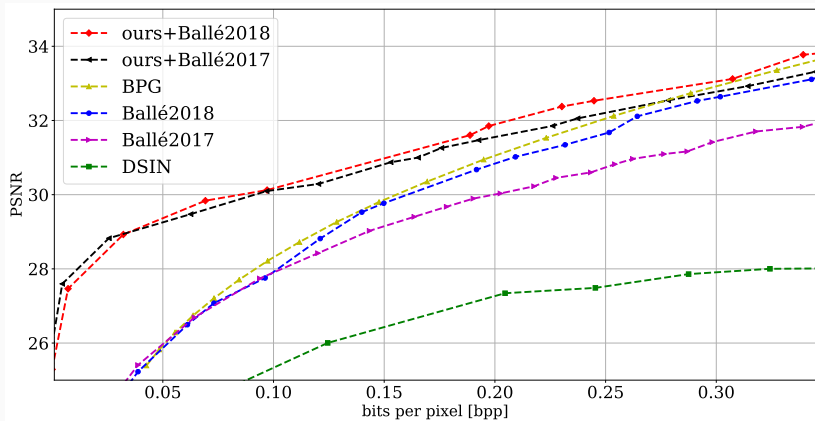
Comparison of different models in terms of PSNR.

Results with KITTI Stereo



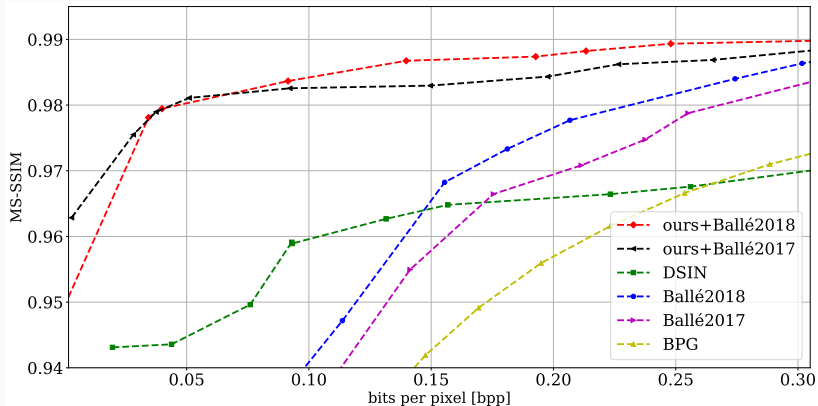
Comparison of different models in terms of MS-SSIM.

Results with Cityscape dataset



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Comparison of different models in terms of MS-SSIM.

Visual Comparisons



(a) Original Image



(b) Ballé2018, $\text{bpp}=0.0261$



(c) DSIN, $\text{bpp} = 0.0187$



(d) Ours, $\text{bpp}=0.0152$



(e) Original Image



(f) Ballé2018, $\text{bpp}=0.0783$



(g) DSIN, $\text{bpp}=0.0588$



(h) Ours, $\text{bpp}=0.0452$



(i) Original Image



(j) Ballé2018, $\text{bpp} = 0.0827$



(k) DSIN, $\text{bpp} = 0.0741$



(l) Ours, $\text{bpp} = 0.0521$

“Ours” refers to “Ours + Ballé2017” model.

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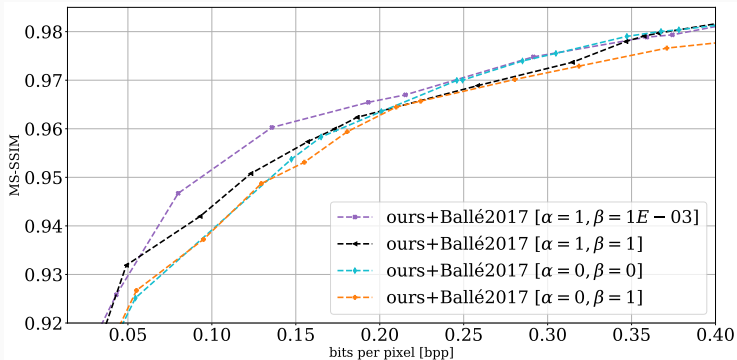


(a) DSIN, $\text{bpp}=0.0449$

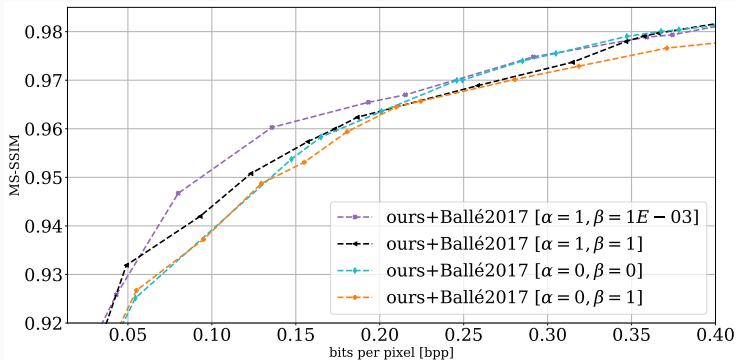


(b) Ours, $\text{bpp}=0.0431$

Effect of hyperparameters α and β



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$$(R_x + \lambda D_x) + \alpha (R_y + \lambda D_y) + \beta R_w$$

Effect of hyperparameters α and β



(a) $\alpha = 1, \beta = 10^{-3}$
bpp = 0.1281



(b) $\alpha = 0, \beta = 0$
bpp = 0.1572



(c) $\alpha = 1, \beta = 1$
bpp = 0.1658



(d) $\alpha = 0, \beta = 1$
bpp = 0.1731

Common information (1st row), private information (2nd row) decomposition, reconstructed images with similar reconstruction quality (3rd row).

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- A novel approach by disentangling common and private information.
- Significant reductions in bit rates by only sending the private information to the decoder.
- Common information consists of global texture and color details, which can be controlled using hyperparameters.

Code publicly available at: <https://github.com/ipc-lab/NDIC>